

## Huiswerk Wiskunde voor Neurale Netwerken

Inleveren 7 oktober om 11:15

1. Consider the following matrices and describe what linear transformations they define.

$$\begin{pmatrix} 1 & 0 \\ 0 & 2 \end{pmatrix} \quad \begin{pmatrix} -1 & 0 \\ 0 & -1 \end{pmatrix} \quad \begin{pmatrix} \cos \alpha & 0 & -\sin \alpha \\ 0 & 1 & 0 \\ \sin \alpha & 0 & \cos \alpha \end{pmatrix}$$

2. Find the matrix of the transformation of symmetry with respect to the line given by vector  $(1, 2)$  in  $\mathbb{R}^2$ .
3. Find the matrix of the rotation in  $\mathbb{R}^3$  with respect to the line given by vector  $(1, 1, 1)$  to the angle  $\alpha$ .
4. Find the rank of the matrix

$$\begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 2 & 4 & 6 \end{pmatrix}$$

5. (a) Check whether the following set is a linear space, motivate your answer.

$$M = \left\{ \begin{pmatrix} 0 \\ a \\ b \end{pmatrix} : a, b \in \mathbb{R} \text{ and } a + b = 1 \right\}$$